## P3 (variant1 and 3)

Q1.

9 (i) Express 
$$\frac{4+5x-x^2}{(1-2x)(2+x)^2}$$
 in partial fractions. [5]

(ii) Hence obtain the expansion of  $\frac{4+5x-x^2}{(1-2x)(2+x)^2}$  in ascending powers of x, up to and including the term in  $x^2$ . [5]

**Q2**.

Expand  $\sqrt[3]{(1-6x)}$  in ascending powers of x up to and including the term in  $x^3$ , simplifying the coefficients. [4]

Q3.

- 2 (i) Expand  $\frac{1}{\sqrt{(1-4x)}}$  in ascending powers of x, up to and including the term in  $x^2$ , simplifying the coefficients. [3]
  - (ii) Hence find the coefficient of  $x^2$  in the expansion of  $\frac{1+2x}{\sqrt{(4-16x)}}$ . [2]

Q4.

1 Expand  $\frac{1}{\sqrt{(4+3x)}}$  in ascending powers of x, up to and including the term in  $x^2$ , simplifying the coefficients. [4]

**Q5**.

2 Expand  $\frac{1+3x}{\sqrt{(1+2x)}}$  in ascending powers of x up to and including the term in  $x^2$ , simplifying the coefficients. [4]

**Q6**.

3 Express 
$$\frac{7x^2 - 3x + 2}{x(x^2 + 1)}$$
 in partial fractions. [5]

Q7.

8 (i) Express 
$$\frac{5x+3}{(x+1)^2(3x+2)}$$
 in partial fractions. [5]

(ii) Hence obtain the expansion of  $\frac{5x+3}{(x+1)^2(3x+2)}$  in ascending powers of x, up to and including the term in  $x^2$ , simplifying the coefficients. [5]

#### **Q8**.

8 Let 
$$f(x) = \frac{3x}{(1+x)(1+2x^2)}$$
.

- (i) Express f(x) in partial fractions. [5]
- (ii) Hence obtain the expansion of f(x) in ascending powers of x, up to and including the term in  $x^3$ .

### Q9.

Expand  $(1 + 2x)^{-3}$  in ascending powers of x, up to and including the term in  $x^2$ , simplifying the coefficients.

#### Q10.

1 Expand  $\frac{16}{(2+x)^2}$  in ascending powers of x, up to and including the term in  $x^2$ , simplifying the coefficients. [4]

### Q11.

When  $(1 + ax)^{-2}$ , where a is a positive constant, is expanded in ascending powers of x, the coefficients of x and  $x^3$  are equal.

(ii) When a has this value, obtain the expansion up to and including the term in x², simplifying the coefficients.
[3]

### Q12.

9 (i) Express 
$$\frac{9-7x+8x^2}{(3-x)(1+x^2)}$$
 in partial fractions. [5]

(ii) Hence obtain the expansion of  $\frac{9-7x+8x^2}{(3-x)(1+x^2)}$  in ascending powers of x, up to and including the term in  $x^3$ .

## Q13.

7 Let 
$$f(x) = \frac{2x^2 - 7x - 1}{(x - 2)(x^2 + 3)}$$
.

- (i) Express f(x) in partial fractions. [5]
- (ii) Hence obtain the expansion of f(x) in ascending powers of x, up to and including the term in  $x^2$ .

#### Q14.

8 (i) Express 
$$\frac{7x^2 + 8}{(1+x)^2(2-3x)}$$
 in partial fractions. [5]

(ii) Hence expand  $\frac{7x^2 + 8}{(1+x)^2(2-3x)}$  in ascending powers of x up to and including the term in  $x^2$ , simplifying the coefficients. [5]

#### Q15.

9 (i) Express 
$$\frac{4+12x+x^2}{(3-x)(1+2x)^2}$$
 in partial fractions. [5]

(ii) Hence obtain the expansion of  $\frac{4+12x+x^2}{(3-x)(1+2x)^2}$  in ascending powers of x, up to and including the term in  $x^2$ . [5]

### Q16.

2 Expand  $(1+3x)^{-\frac{1}{3}}$  in ascending powers of x, up to and including the term in  $x^3$ , simplifying the coefficients. [4]

### Q17.

9 Let 
$$f(x) = \frac{x^2 - 8x + 9}{(1 - x)(2 - x)^2}$$
.

- (i) Express f(x) in partial fractions. [5]
- (ii) Hence obtain the expansion of f(x) in ascending powers of x, up to and including the term in  $x^2$ .