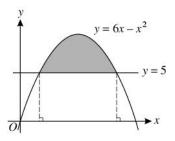


Q1.

4



The diagram shows the curve  $y = 6x - x^2$  and the line y = 5. Find the area of the shaded region. [6]

Q2.

The equation of a curve is such that  $\frac{dy}{dx} = \frac{6}{\sqrt{(3x-2)}}$ . Given that the curve passes through the point P(2, 11), find

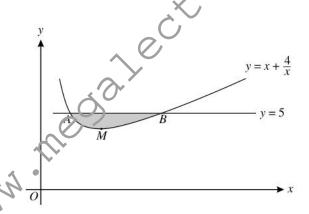
(i) the equation of the normal to the curve at P, [3]

(ii) the equation of the curve.

[4]

Q3.

9



The diagram shows part of the curve  $y = x + \frac{4}{x}$  which has a minimum point at M. The line y = 5 intersects the curve at the points A and B.

(i) Find the coordinates of A, B and M. [5]

(ii) Find the volume obtained when the shaded region is rotated through 360° about the x-axis. [6]

Q4.

3 (i) Sketch the curve  $y = (x-2)^2$ . [1]

(ii) The region enclosed by the curve, the x-axis and the y-axis is rotated through 360° about the x-axis. Find the volume obtained, giving your answer in terms of  $\pi$ . [4]



Q5.

7 A curve is such that  $\frac{dy}{dx} = \frac{3}{(1+2x)^2}$  and the point  $(1, \frac{1}{2})$  lies on the curve.

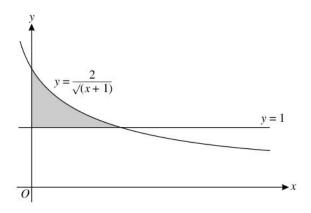
- (i) Find the equation of the curve. [4]
- (ii) Find the set of values of x for which the gradient of the curve is less than  $\frac{1}{3}$ . [3]

Q6.

- 9 A curve is such that  $\frac{dy}{dx} = \frac{2}{\sqrt{x}} 1$  and P(9, 5) is a point on the curve.
  - (i) Find the equation of the curve. [4]
  - (ii) Find the coordinates of the stationary point on the curve. [3]
  - (iii) Find an expression for  $\frac{d^2y}{dx^2}$  and determine the nature of the stationary point. [2]
  - (iv) The normal to the curve at P makes an angle of  $\tan^{-1} k$  with the positive x-axis. Find the value of k.

Q7.

11



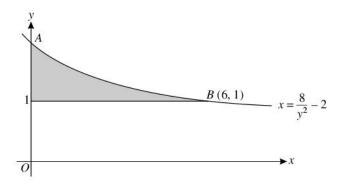
The diagram shows the line y = 1 and part of the curve  $y = \frac{2}{\sqrt{(x+1)}}$ .

- (i) Show that the equation  $y = \frac{2}{\sqrt{(x+1)}}$  can be written in the form  $x = \frac{4}{y^2} 1$ . [1]
- (ii) Find  $\int \left(\frac{4}{y^2} 1\right) dy$ . Hence find the area of the shaded region. [5]
- (iii) The shaded region is rotated through 360° about the *y*-axis. Find the exact value of the volume of revolution obtained. [5]

**Q8**.



5



The diagram shows part of the curve  $x = \frac{8}{y^2} - 2$ , crossing the y-axis at the point A. The point B (6, 1) lies on the curve. The shaded region is bounded by the curve, the y-axis and the line y = 1. Find the exact volume obtained when this shaded region is rotated through 360° about the y-axis. [6]

Q9.

9 A curve is such that  $\frac{d^2y}{dx^2} = -4x$ . The curve has a maximum point at (2, 12).

(i) Find the equation of the curve.

[6]

A point P moves along the curve in such a way that the recordinate is increasing at 0.05 units per second.

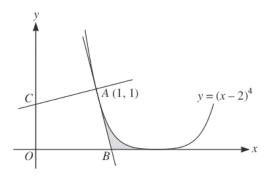
(ii) Find the rate at which the y-coordinate is changing when x = 3, stating whether the y-coordinate is increasing or decreasing. [2]

Q10.

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10



The diagram shows part of the curve  $y = (x - 2)^4$  and the point A(1, 1) on the curve. The tangent at A cuts the x-axis at B and the normal at A cuts the y-axis at C.

(i) Find the coordinates of B and C. [6]

(ii) Find the distance AC, giving your answer in the form  $\frac{\sqrt{a}}{b}$ , where a and b are integers. [2]

(iii) Find the area of the shaded region. [4]

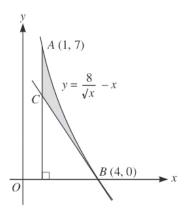
Q11.

A curve is such that  $\frac{dy}{dx} = \sqrt{(2x+5)}$  and (2, 5) is a point on the curve. Find the equation of the curve.

Q12.



11



The diagram shows part of the curve  $y = \frac{8}{\sqrt{x}} - x$  and points A(1, 7) and B(4, 0) which lie on the curve. The tangent to the curve at B intersects the line x = 1 at the point C.

(i) Find the coordinates of C.

[4]

(ii) Find the area of the shaded region.

[5]

Q13.

A curve is such that  $\frac{dy}{dx} = k - 2x$ , where k is a constant.

(i) Given that the tangents to the curve at the points where x = 2 and x = 3 are perpendicular, find

The c

(ii) Given also that the curve passes through the point (4, 9), find the equation of the curve. [3]

Q14.

1 Find 
$$\int \left(x + \frac{1}{x}\right)^2 dx$$
. [3]

Q15.

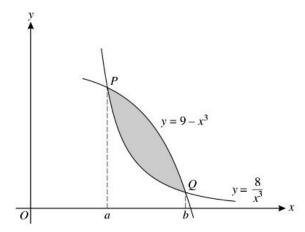
The equation of a curve is  $y = \frac{3}{2-x}$ .

- (i) Find an expression for  $\frac{dy}{dx}$  and determine, with a reason, whether the curve has any stationary
- (ii) Find the volume obtained when the region bounded by the curve, the coordinate axes and the line x = 1 is rotated through 360° about the x-axis.
- (iii) Find the set of values of k for which the line y = x + k intersects the curve at two distinct points.

Q16.



11



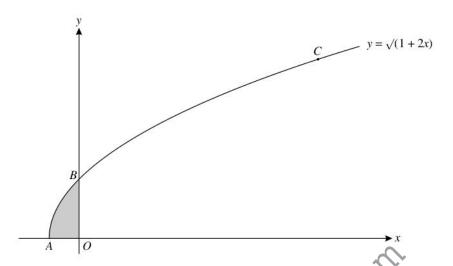
The diagram shows parts of the curves  $y = 9 - x^3$  and  $y = \frac{8}{x^3}$  and their points of intersection P and Q. The x-coordinates of P and Q are a and b respectively.

- (i) Show that x = a and x = b are roots of the equation  $x^6 9x^3 + 8 = 0$ . Solve this equation and hence state the value of a and the value of b. [4]
- (ii) Find the area of the shaded region between the two curves.
  [5]
- (iii) The tangents to the two curves at x = c (where a < c < b) are parallel to each other. Find the value of c.

Q17.



10



The diagram shows the curve  $y = \sqrt{1 + 2x}$  meeting the x-axis at A and the y-axis at B. The y-coordinate of the point C on the curve is 3.

(i) Find the coordinates of B and C.

[2]

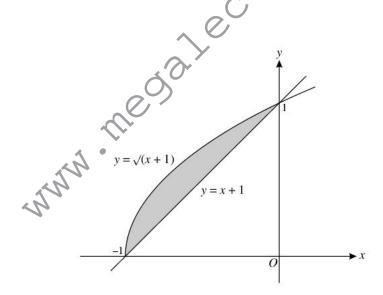
(ii) Find the equation of the normal to the curve at C.

[4]

(iii) Find the volume obtained when the shaded region is rotated through  $360^{\circ}$  about the y-axis. [5]

Q18.

10



The diagram shows the line y = x + 1 and the curve  $y = \sqrt{(x + 1)}$ , meeting at (-1, 0) and (0, 1).

(i) Find the area of the shaded region.

[5]

(ii) Find the volume obtained when the shaded region is rotated through 360° about the y-axis. [7]

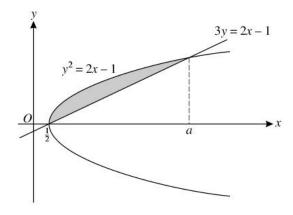
Q19.



2 A curve is such that  $\frac{dy}{dx} = -\frac{8}{x^3} - 1$  and the point (2, 4) lies on the curve. Find the equation of the curve.

Q20.

8



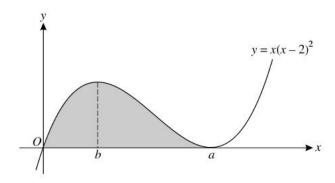
The diagram shows the curve  $y^2 = 2x - 1$  and the straight line 3y = 2x - 1. The curve and straight line intersect at  $x = \frac{1}{2}$  and x = a, where a is a constant.

- (i) Show that a = 5. [2]
- (ii) Find, showing all necessary working, the area of the shaded region. [6]

Q21.



11



The diagram shows the curve with equation  $y = x(x-2)^2$ . The minimum point on the curve has coordinates (a, 0) and the x-coordinate of the maximum point is b, where a and b are constants.

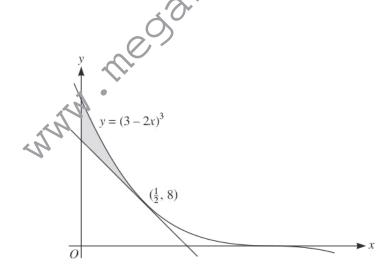
- (i) State the value of a.
- (ii) Find the value of b. [4]
- (iii) Find the area of the shaded region. [4]
- (iv) The gradient,  $\frac{dy}{dx}$ , of the curve has a minimum value m. Find the value of m. [4]

Q22.

2 A curve has equation y = f(x). It is given that  $f'(x) = \frac{1}{\sqrt{(x+6)}} + \frac{6}{x^2}$  and that f(3) = 1. Find f(x). [5]

Q23.

10



The diagram shows the curve  $y = (3 - 2x)^3$  and the tangent to the curve at the point  $(\frac{1}{2}, 8)$ .

- (i) Find the equation of this tangent, giving your answer in the form y = mx + c. [5]
- (ii) Find the area of the shaded region. [6]

[1]

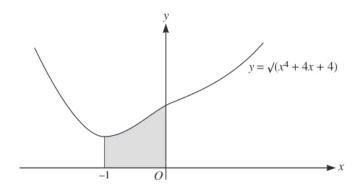


Q24.

2 A curve has equation y = f(x). It is given that  $f'(x) = x^{-\frac{3}{2}} + 1$  and that f(4) = 5. Find f(x). [4]

Q25.

11



The diagram shows the curve  $y = \sqrt{(x^4 + 4x + 4)}$ .

- (i) Find the equation of the tangent to the curve at the point (0, 2). [4]
- (ii) Show that the x-coordinates of the points of intersection of the line y = x + 2 and the curve are given by the equation  $(x + 2)^2 = x^4 + 4x + 4$ . Hence find these x-coordinates. [4]
- (iii) The region shaded in the diagram is rotated through 360° about the x-axis. Find the volume of revolution. [4]



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