

Chapter 2 Logarithmic and Exponential functions

Oct/Nov 2002

- 3 (i) Show that the equation

$$\log_{10}(x + 5) = 2 - \log_{10} x$$

may be written as a quadratic equation in x .

[3]

- (ii) Hence find the value of x satisfying the equation

$$\log_{10}(x + 5) = 2 - \log_{10} x.$$

[2]

Oct/Nov 2003

- 1 Solve the inequality $|2^x - 8| < 5$.

[4]

May/June 2004

- 4 (i) Show that if $y = 2^x$, then the equation

$$2^x - 2^{-x} = 1$$

can be written as a quadratic equation in y .

[2]

- (ii) Hence solve the equation

$$2^x - 2^{-x} = 1.$$

[4]

Oct/Nov 2004

- 2 Solve the equation

$$\ln(1 + x) = 1 + \ln x,$$

giving your answer correct to 2 significant figures.

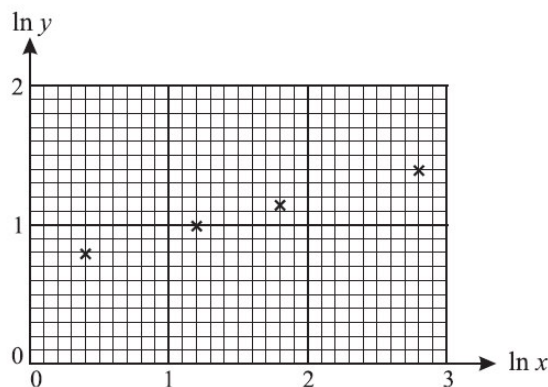
[4]

May/June 2005

- 1 Given that $x = 4(3^{-y})$, express y in terms of x .

[3]

2



Two variable quantities x and y are related by the equation $y = Ax^n$, where A and n are constants. The diagram shows the result of plotting $\ln y$ against $\ln x$ for four pairs of values of x and y . Use the diagram to estimate the values of A and n .

[5]

May/June 2007

- 4 Using the substitution $u = 3^x$, or otherwise, solve, correct to 3 significant figures, the equation

$$3^x = 2 + 3^{-x}. \quad [6]$$

May/June 2008

- 2 Solve, correct to 3 significant figures, the equation

$$e^x + e^{2x} = e^{3x}. \quad [5]$$

Oct/Nov 2008

- 1 Solve the equation

$$\ln(x + 2) = 2 + \ln x,$$

giving your answer correct to 3 decimal places. [3]

May/June 2009

- 1 Solve the equation $\ln(2 + e^{-x}) = 2$, giving your answer correct to 2 decimal places. [4]

Oct/Nov 2009/31

- 2 Solve the equation $3^{x+2} = 3^x + 3^2$, giving your answer correct to 3 significant figures. [4]

Oct/Nov 2009/32

- 1 Solve the equation

$$\ln(5 - x) = \ln 5 - \ln x,$$

giving your answers correct to 3 significant figures. [4]

May/June 2010/31

- 3 The variables x and y satisfy the equation $x^n y = C$, where n and C are constants. When $x = 1.10$, $y = 5.20$, and when $x = 3.20$, $y = 1.05$.

(i) Find the values of n and C . [5]

(ii) Explain why the graph of $\ln y$ against $\ln x$ is a straight line. [1]

May/June 2010/32

- 1 Solve the equation

$$\frac{2^x + 1}{2^x - 1} = 5,$$

giving your answer correct to 3 significant figures. [4]

May/June 2010/33

- 2 The variables x and y satisfy the equation $y^3 = Ae^{2x}$, where A is a constant. The graph of $\ln y$ against x is a straight line.
- (i) Find the gradient of this line. [2]
- (ii) Given that the line intersects the axis of $\ln y$ at the point where $\ln y = 0.5$, find the value of A correct to 2 decimal places. [2]